

# Observational tests of an inhomogeneous cosmology

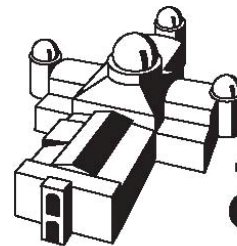
*by Christoph Saulder*

in cooperation with Steffen Mieske & Werner Zeilinger



European  
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Observatory

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institut für  
astronomie

UNIVERSITÄTSSTERNWARTE WIEN

# A review of basic cosmology

- Cosmology → applied General Relativity

- Einstein's field equation

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

- Cosmological principle:

**homogeneity and isotropy**

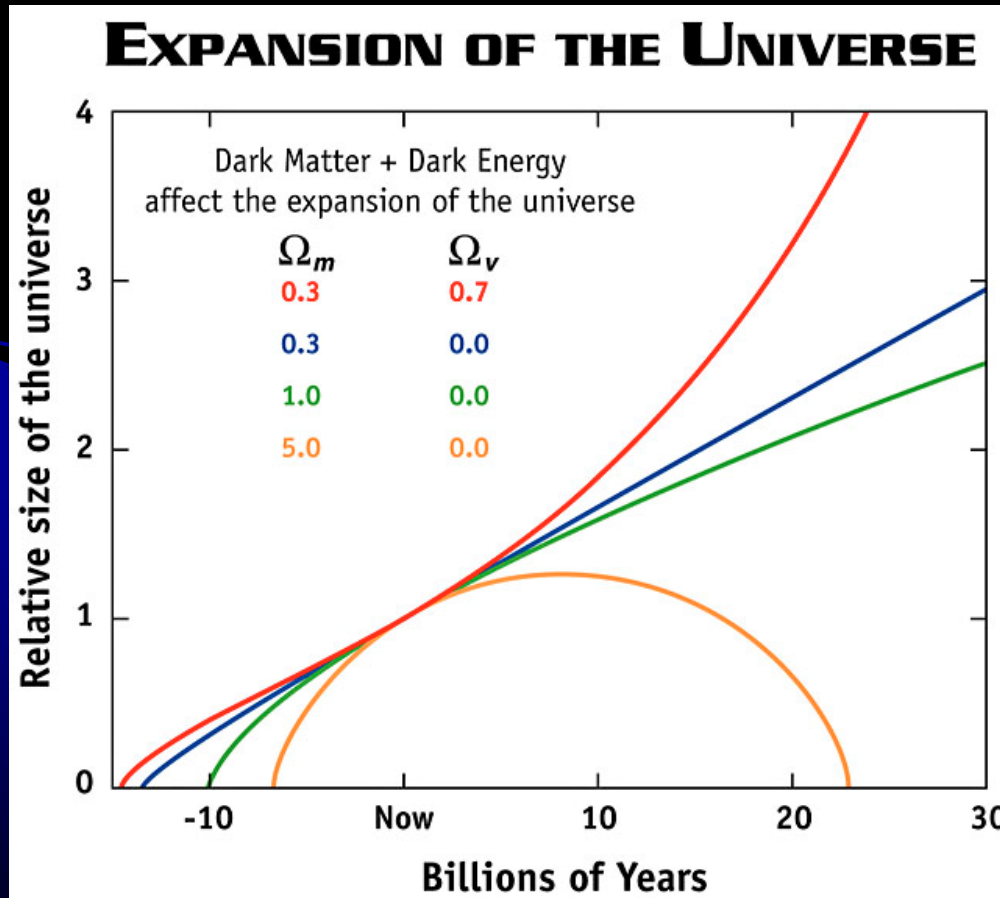
- Friedmann-Lemaître-Robertson-Walker metric

$$ds^2 = c^2 dt^2 - a(t)^2 \left[ dr^2 + f(r) \left[ d\theta^2 + \sin(\theta) d\varphi^2 \right] \right]$$

Friedmann equations:

$$H^2 = \left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi G}{3c^2} \rho - \frac{Kc^2}{a^2}$$

$$\dot{H} + H^2 = \frac{\ddot{a}}{a} = -\frac{4\pi G}{3c^2} (\rho + 3p)$$



Written using energy densities:

$$\frac{H^2}{H_0^2} = \Omega_\gamma a^{-4} + \Omega_M a^{-3} + \Omega_k a^{-2} + \Omega_\Lambda$$

Observed accelerated expansion due to **Dark Energy?**

# Timescape cosmology

- The universe isn't homogeneous  
→ voids and clusters
- General relativity is a non-linear theory.
- The averaging on large scales has to be modified.
- Back reaction from inhomogeneities expected.

- **Perturbative approach: Buchert's scheme (Buchert 2000)**

$$3\left(\frac{\dot{\bar{a}}}{\bar{a}}\right)^2 = 8\pi G \langle \rho \rangle - \frac{1}{2} \langle R \rangle - \frac{1}{2} Q$$

$$3\frac{\ddot{\bar{a}}}{\bar{a}} = -4\pi G \langle \rho \rangle + Q$$

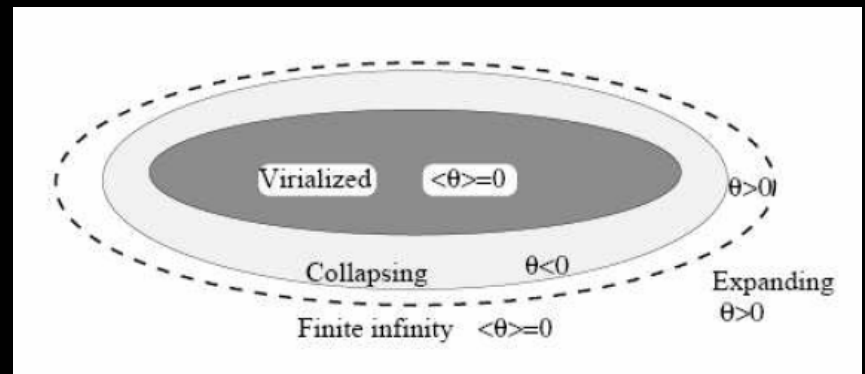
$$\partial_t \langle \rho \rangle + 3\frac{\dot{\bar{a}}}{\bar{a}} \langle \rho \rangle = 0$$

$$Q = \frac{2}{3} \langle (\theta - \langle \theta \rangle)^2 \rangle - 2 \langle \sigma \rangle^2$$

- **Perturbation theory alone is not sufficient (Räsänen, 2006)**

- Importance of local metric, abolishing the universal time parameter in cosmology → timescape cosmology (Wiltshire, 2007)

- two phase model
- Separated by a finite infinity boundary



by Wiltshire, 2007

- Walls have a renormalized critical density
- Voids are empty
- We are in wall environment
  - ➔ our observations of the global parameters of the universe have to be recalibrated

- Nowadays the universe is dominated by voids.
- Different expansion rates in different environments due to the local metric.
- Voids expand faster than walls
- ➔ **accelerated expansion of the universe**  
(no Dark Energy required anymore)

$$\left(\frac{\dot{\bar{a}}}{\bar{a}}\right)^2 + \frac{\dot{f}_v^2}{9f_v(1-f_v)} - \frac{\alpha^2 f_v^{1/3}}{\bar{a}^2} = \frac{8\pi G}{3} \bar{\rho}_0 \frac{\bar{a}_0^3}{\bar{a}^3}$$

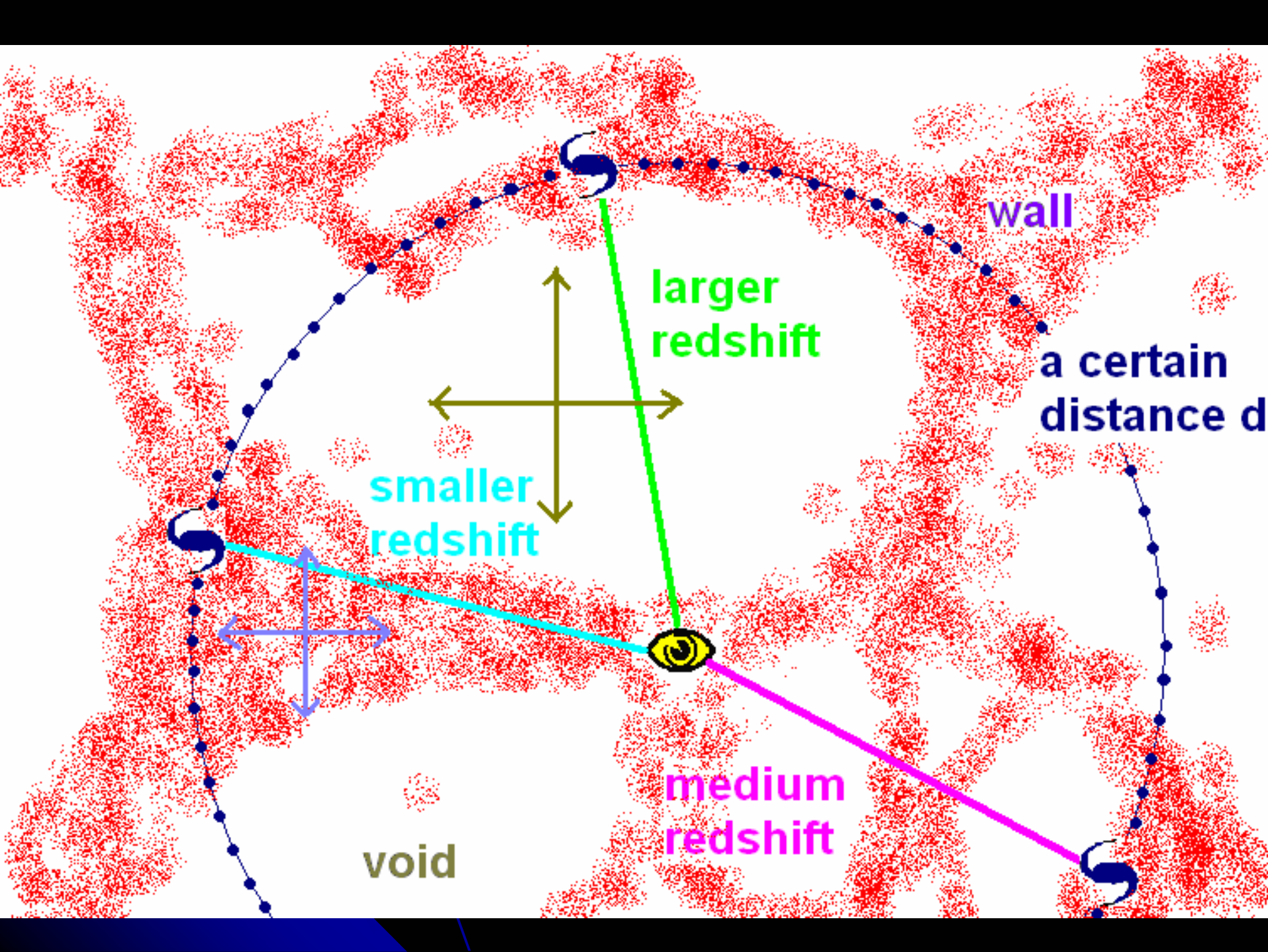
$$\ddot{f}_v + \frac{\dot{f}_v^2(2f_v-1)}{2f_v(1-f_v)} + 3\frac{\dot{\bar{a}}}{\bar{a}}\dot{f}_v - \frac{3\alpha^2 f_v^{1/3}(1-f_v)}{2\bar{a}^2} = 0$$

Wiltshire, 2007

# Observational features

- CMB-power spectrum, cosmic rays, ...
- different Hubble parameters depending on the environment:
  - void regions expand about 15-20%(?)  
faster than wall regions
- observed Hubble parameter should depend on the foreground (fraction of wall regions in the line of sight) (Schwarz 2010)
- effect averages out at the scale of homogeneity





- optimal distance between 50 and 200 Mpc
- requires redshift and another independent distance indicator, like the fundamental plane
- lots of data required
- homogenous sample on a large area of the sky:  
e.g. elliptical galaxies from SDSS
- one also has to model the foreground

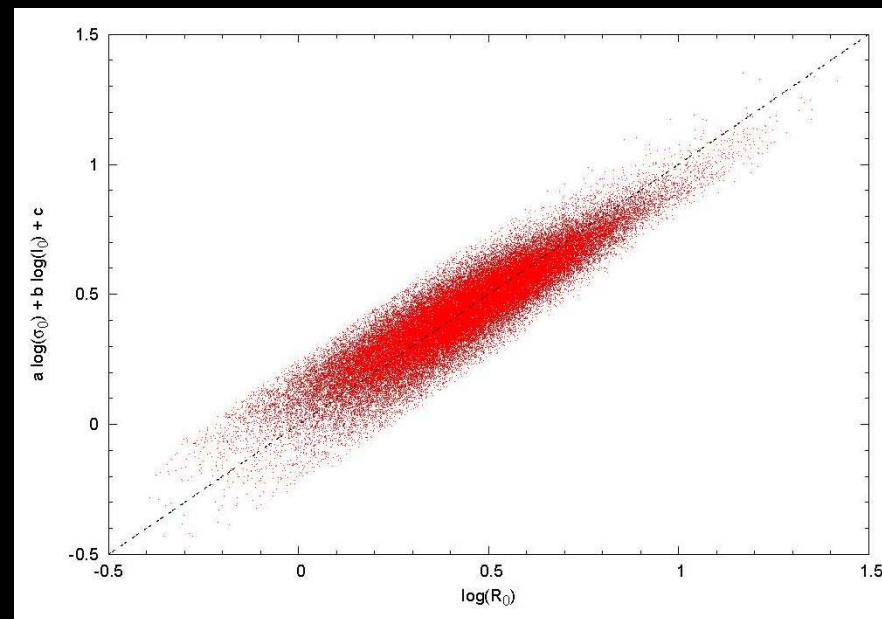
# Data sources

- Sloan Digital Sky Survey (SDSS) DR8
  - Photometric data (model magnitudes and effective radii in 5 different filters and)
  - Extinction map (Schlegel et al. 1998)
  - Spectroscopic data (redshift, central velocity dispersion)
- GalaxyZoo (SDSS-based citizen science project for galaxy classification - Lintott et al. 2008 & 2010)
- Masses from the (SDSS-based) catalog of groups and clusters by Yang et al., 2008

# Performing the test

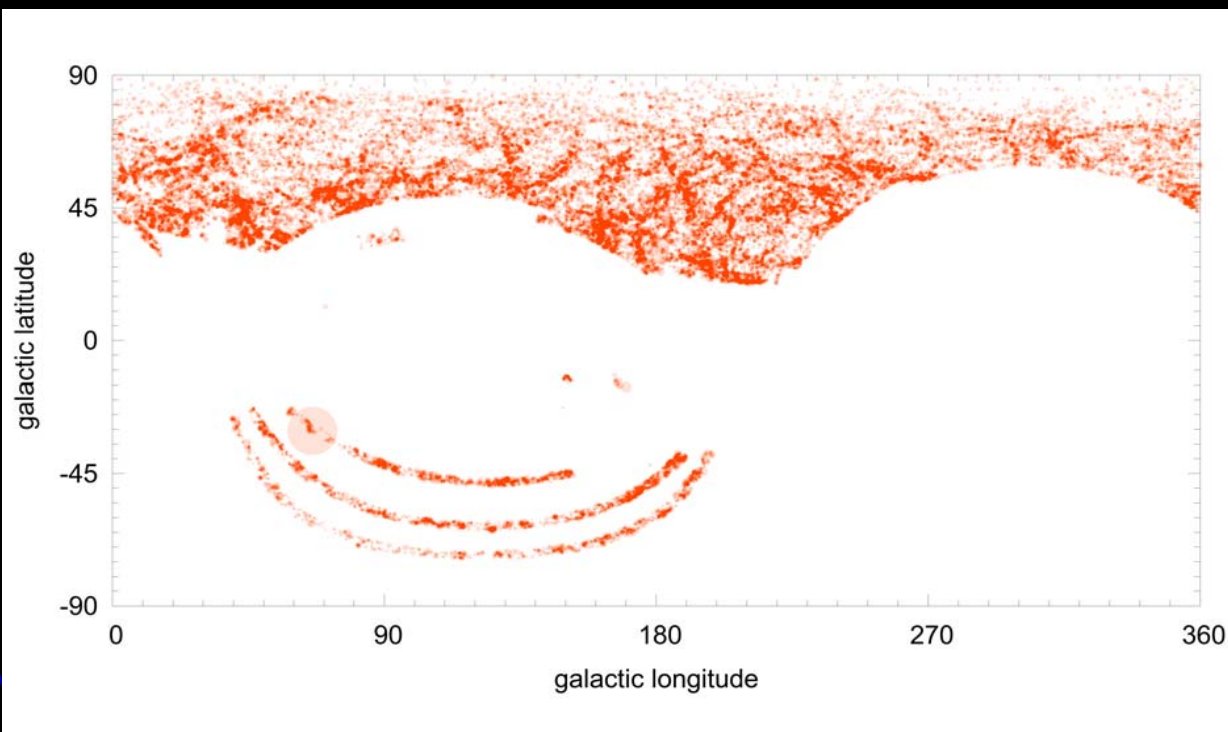
- Recalibrating the fundamental plane
  - 70000 elliptical galaxies from SDSS
  - classified by GalaxyZoo (+additional constraints)
  - redshift range [0 , 0.15]
  - using a new high quality K-correction (Chilingarian et al. 2010)
  - RMS in SDSS r-band <10%

$$\log(R_0) = a \cdot \log(\sigma_{cor}) + b \cdot \log(I_0) + c$$



# ● Modeling the foreground

- Getting positions, redshift based distances of more than 350 000 galaxies from SDSS
- Masses from Yang et al. 2008 (SDSS DR4 based) or estimated from mass/light ratios
- Homogeneous spheres with a renormalized critical density

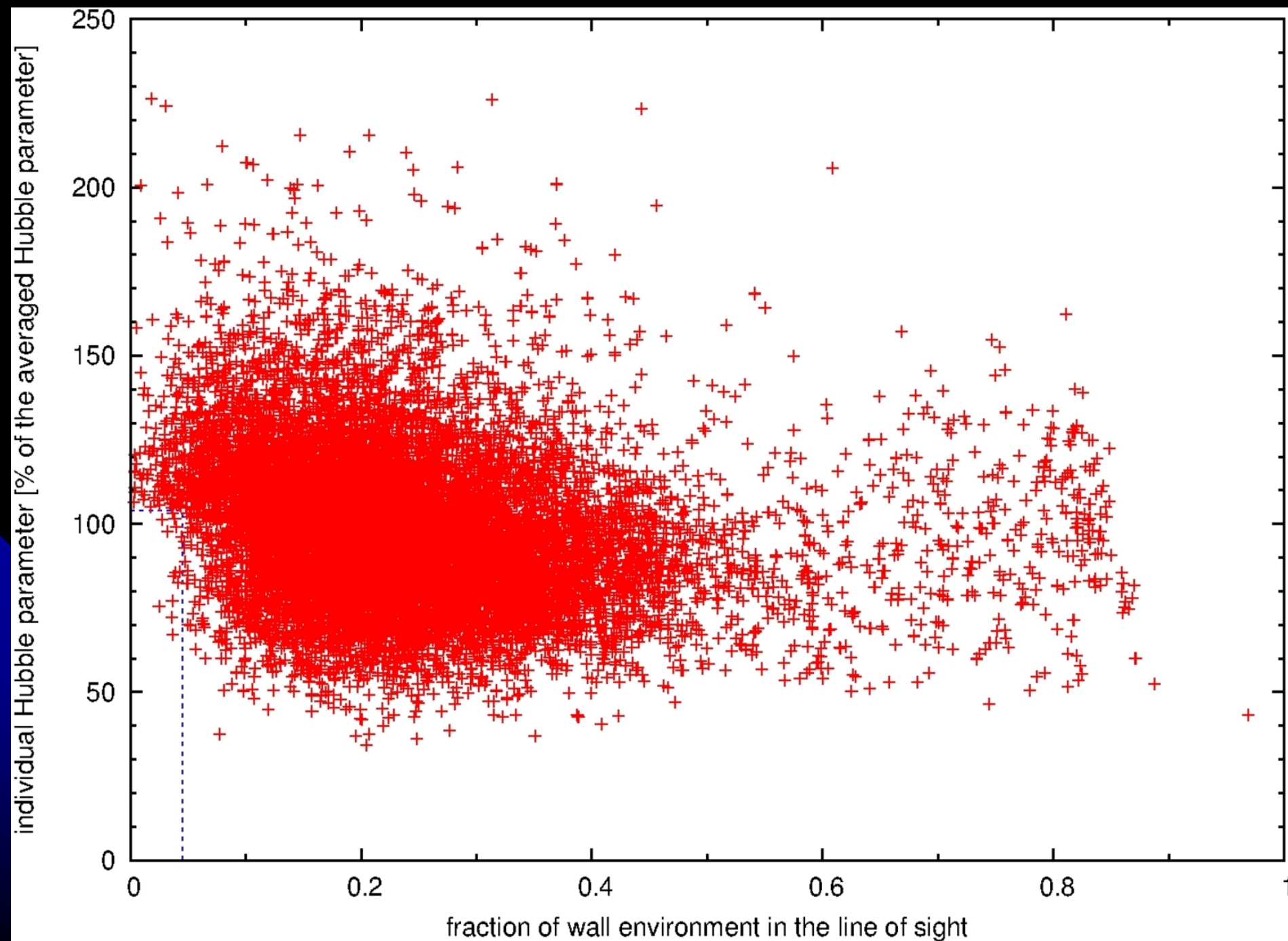


A part of the foreground model  
between 100 and 150  $h^{-1}$  Mpc



# ● Final analysis

- Calculate the “individual Hubble-parameters” of a quality selected sample of about 10 000 elliptical galaxies with  $z < 0.1$  using the **fundamental plane distances** and the **redshift** from SDSS
- Calculate fraction inside finite infinity region by intersecting the spheres with the line of sight to those galaxies.
- Compare them and make a **plot**.



# Summary

- Using the fundamental plane to calculate distances
  - ➔ additional output: new coefficients for the fundamental plane
- Comparing distances and redshifts
  - ➔ additional output: peculiar motions
- The foreground model
  - ➔ additional output: masses of clusters and galaxies + peculiar motions



- Testing timescape cosmology
- First results look promising, but there still several open questions in our models.
- Positive results would be a major discovery.
- Intermediate results would favor Dark Energy theories with a Chameleon effect such as  $f(R)$  modified gravity.
- Negative results would support the  $\Lambda$ -CDM.

**CAST LIGHT ON DARK ENERGY**

**ANY  
QUESTIONS?**

